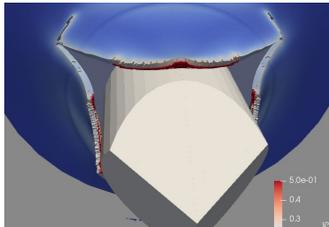




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NNM Force Appropriation Pre-test Prediction of Assembly using Calibrated Component and Modal Shaker Models



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I. Introduction



- Despite its effect on multiple aspects of structural dynamics, nonlinearity is under-considered and often neglected in industrial design and qualification
- To develop understanding of nonlinear structural dynamics, Siemens Industry Software attempted system identification on a demo aluminum aircraft (Fig. 1) [1]
- But, dynamics of the full system (wing+pylon+fixture) were too complex

Solution: Begin with isolated fixture-pylon structure

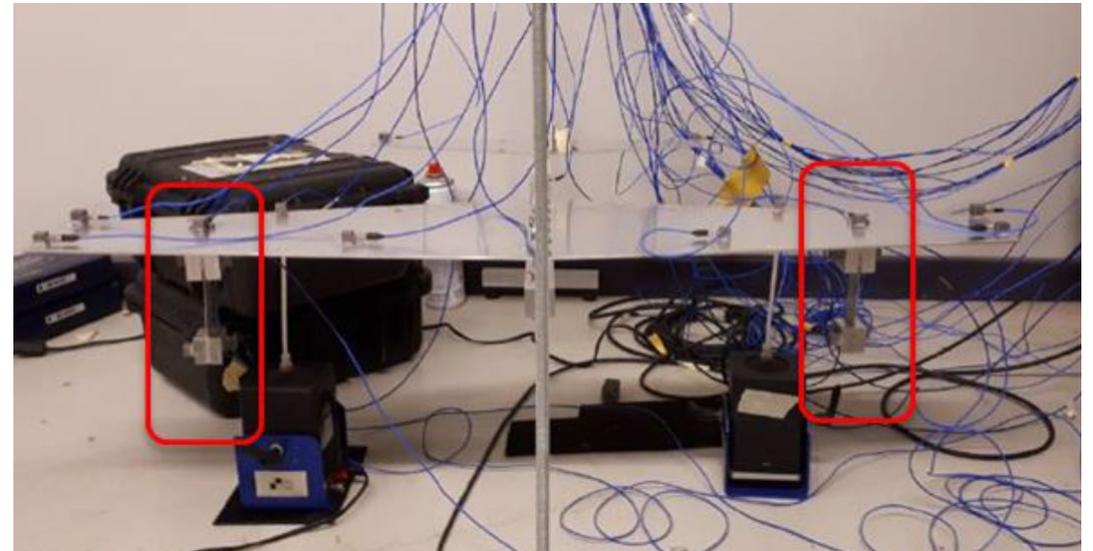


Fig. 1: Siemens demo aluminum aircraft [1]

- A NOMAD 2019 research group studied the isolated fixture-pylon structure [2]
- Experiments were conducted on the setup shown in Fig. 2
 - Shaker was used to excite fixture-pylon structure
 - Data collected through accelerometers

Results:

Experimental data

Basic nonlinear model

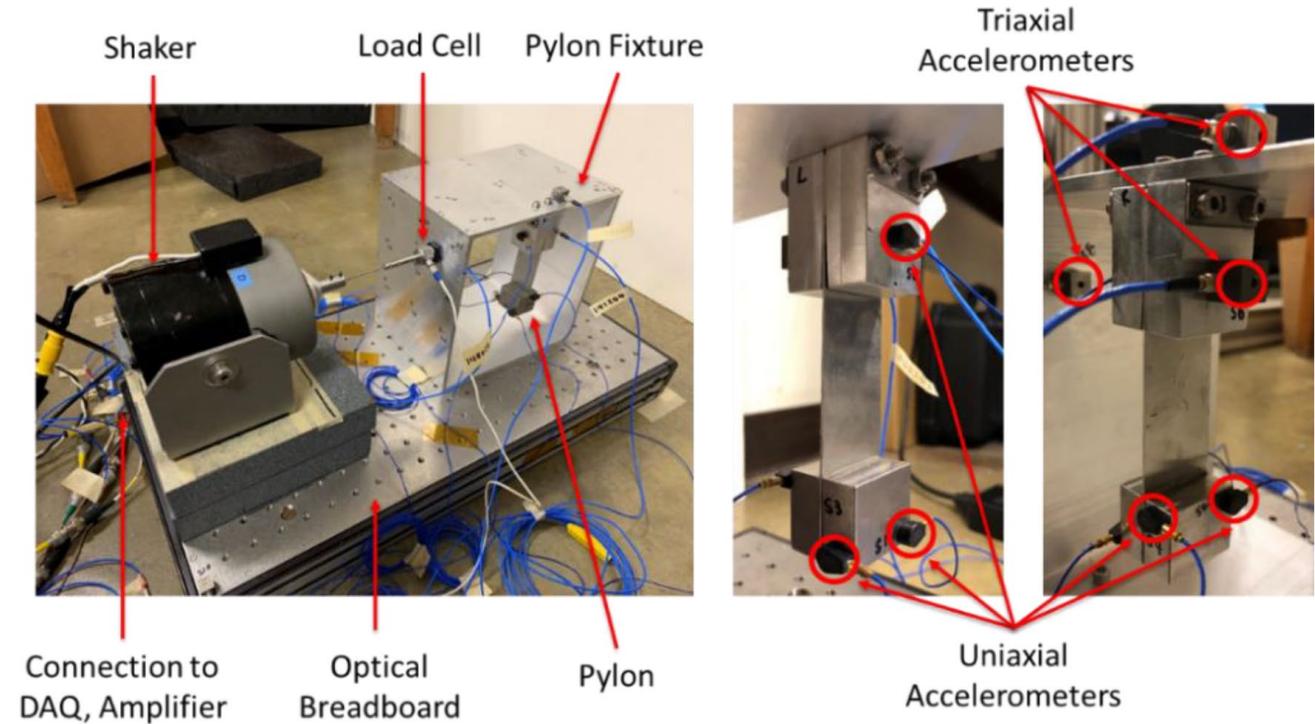


Fig. 2: Sandia isolated fixture-pylon test setup

The NOMAD 2020 project builds upon the previous results by:

- Analyzing experimental data
- Further developing the nonlinear model of the fixture-pylon assembly
- Calibrating fixture-pylon model against experimental data
- Combining fixture-pylon model with linear model of the wing structure
- Analyzing the fixture-pylon and wing-pylon-fixture models
- Simulating experiments by coupling wing-pylon model to a shaker model

First step: Analyzing fixture-pylon experimental data

Previous experiments resulted in sine spectra data from accelerometers

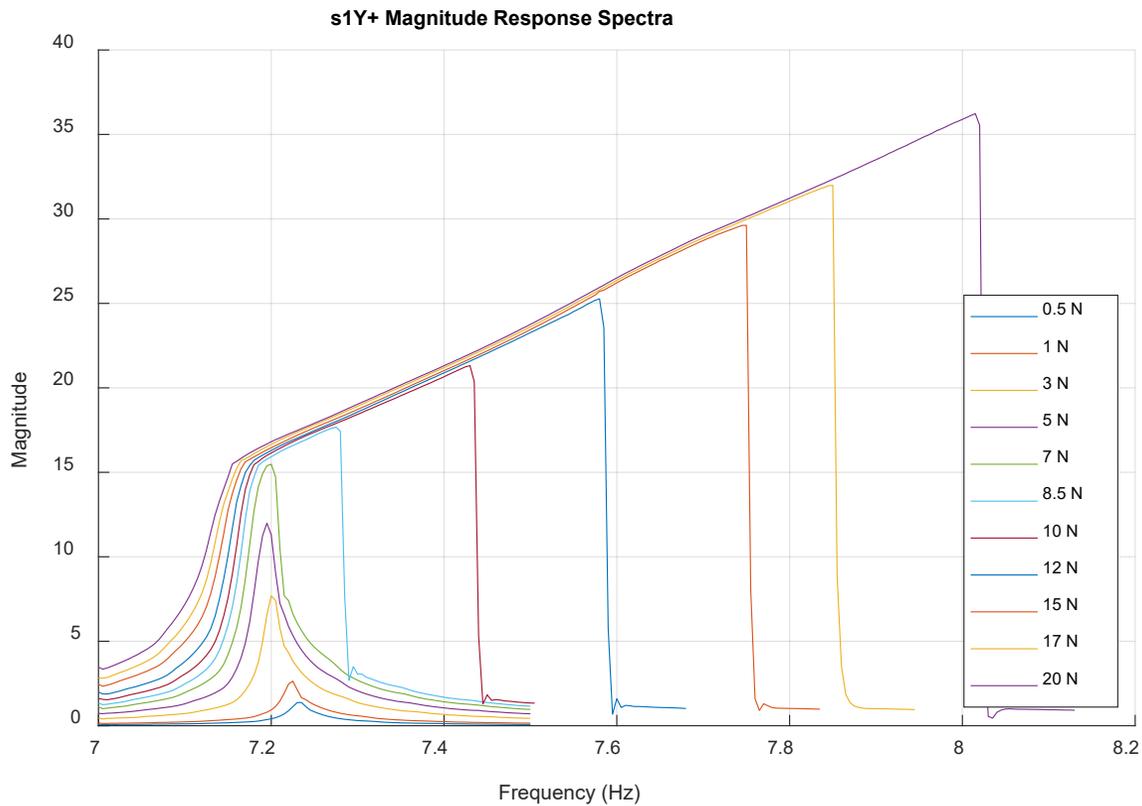


Fig. 3: Sine spectra magnitude response

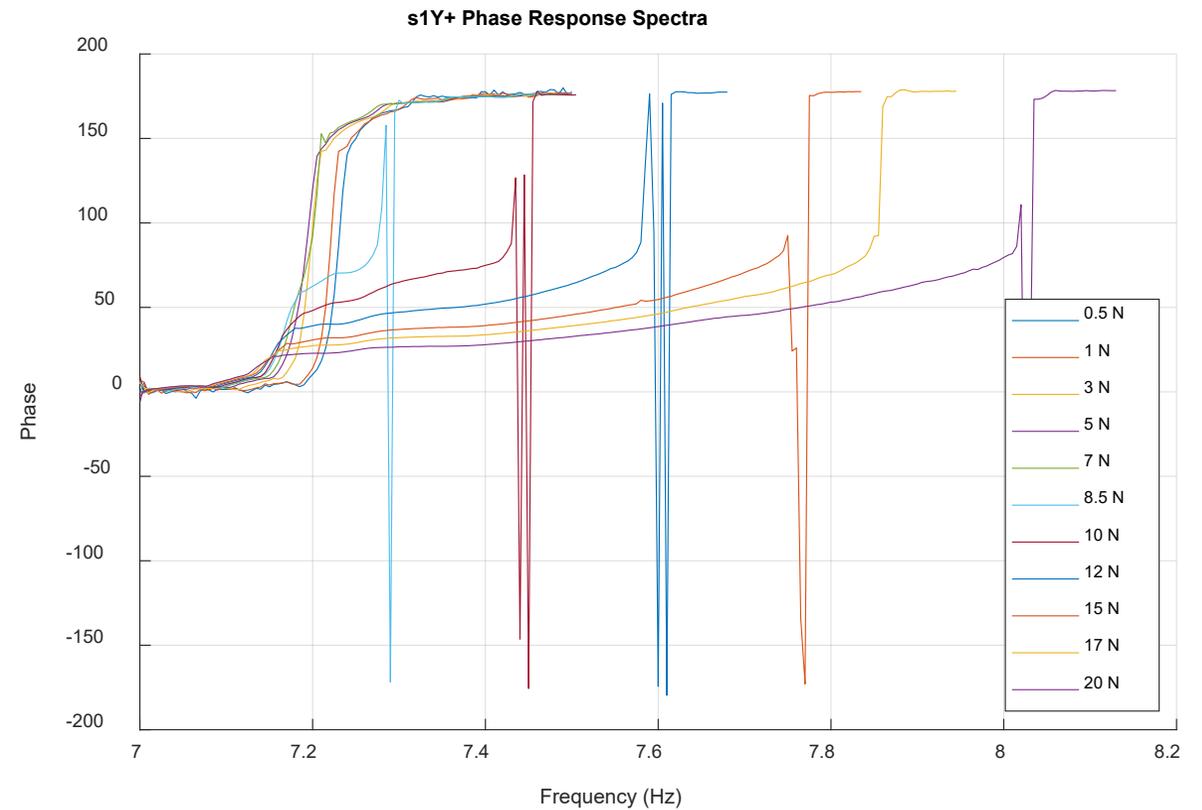


Fig. 4: Sine spectra phase response



From test data, we extracted backbone curves

- Backbone curves are a useful tool for understanding nonlinear behavior
- Backbone aligned with peaks of magnitude response

Backbone curves

=

Starting point

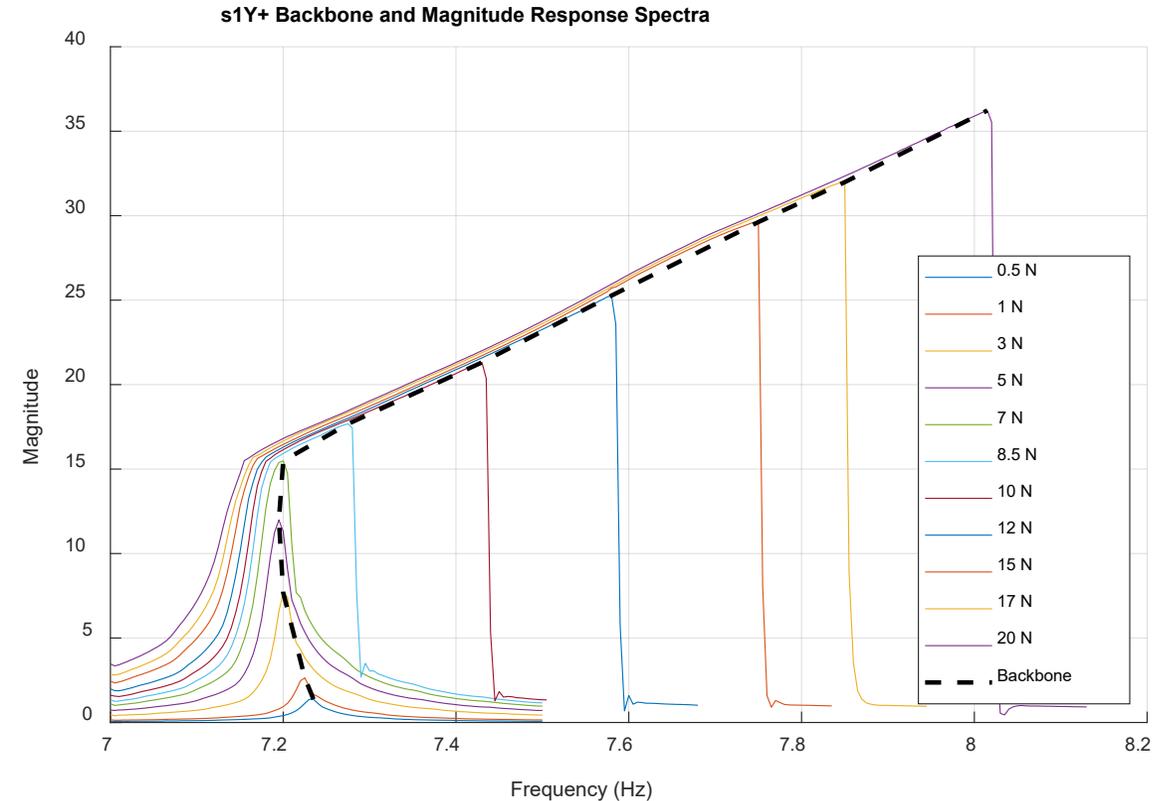


Fig. 5: *s1Y+* backbone curve and magnitude response from sine spectra experimental data



II. Fixture-Pylon Assembly



Fixture-Pylon ROM



- To compare the experimental data to a numerical model, a linear finite element model was created for the fixture-pylon assembly using CUBIT
- To reduce the degrees of freedom (DOFs) in the model, a Craig-Bampton (CB) reduction was run in Sierra SD to obtain a reduced order model (ROM) [3-4]
 - This takes the full model with thousands of DOFs and reduces it to a more manageable model with only 7 retained DOFs (virtual nodes, accelerometers, and drive point)

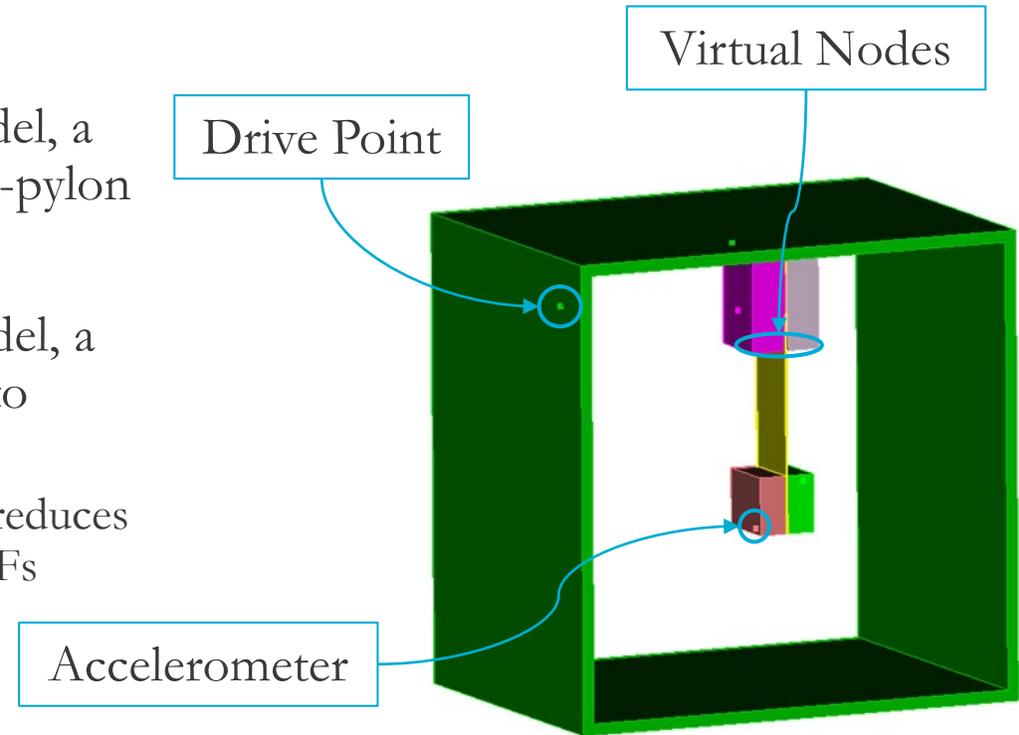


Fig. 6: Fixture-pylon CAD assembly

Reduce the full model to something more manageable:

Full model → CB reduction → Linear ROM

Fixture-Pylon ROM (cont.)



- The linear ROM from Sierra provides the mass and stiffness matrices for the fixture-pylon
 - Damping matrix is computed using proportional damping
- To convert the linear ROM to a nonlinear model, virtual nodes were tied to the pylon block so that a nonlinear restoring force could be added to the equations of motion (EOMs)
- EOMs of nonlinear dynamic system:

$$\underbrace{M\ddot{x}(t) + C\dot{x}(t) + Kx(t)}_{\text{Linear ROM (Sierra Output)}} + \underbrace{f_{nl}\{x(t)\}}_{\text{Nonlinear restoring force between virtual nodes (MATLAB)}} = u$$

Linear ROM
(Sierra Output)

Nonlinear restoring force
between virtual nodes
(MATLAB)

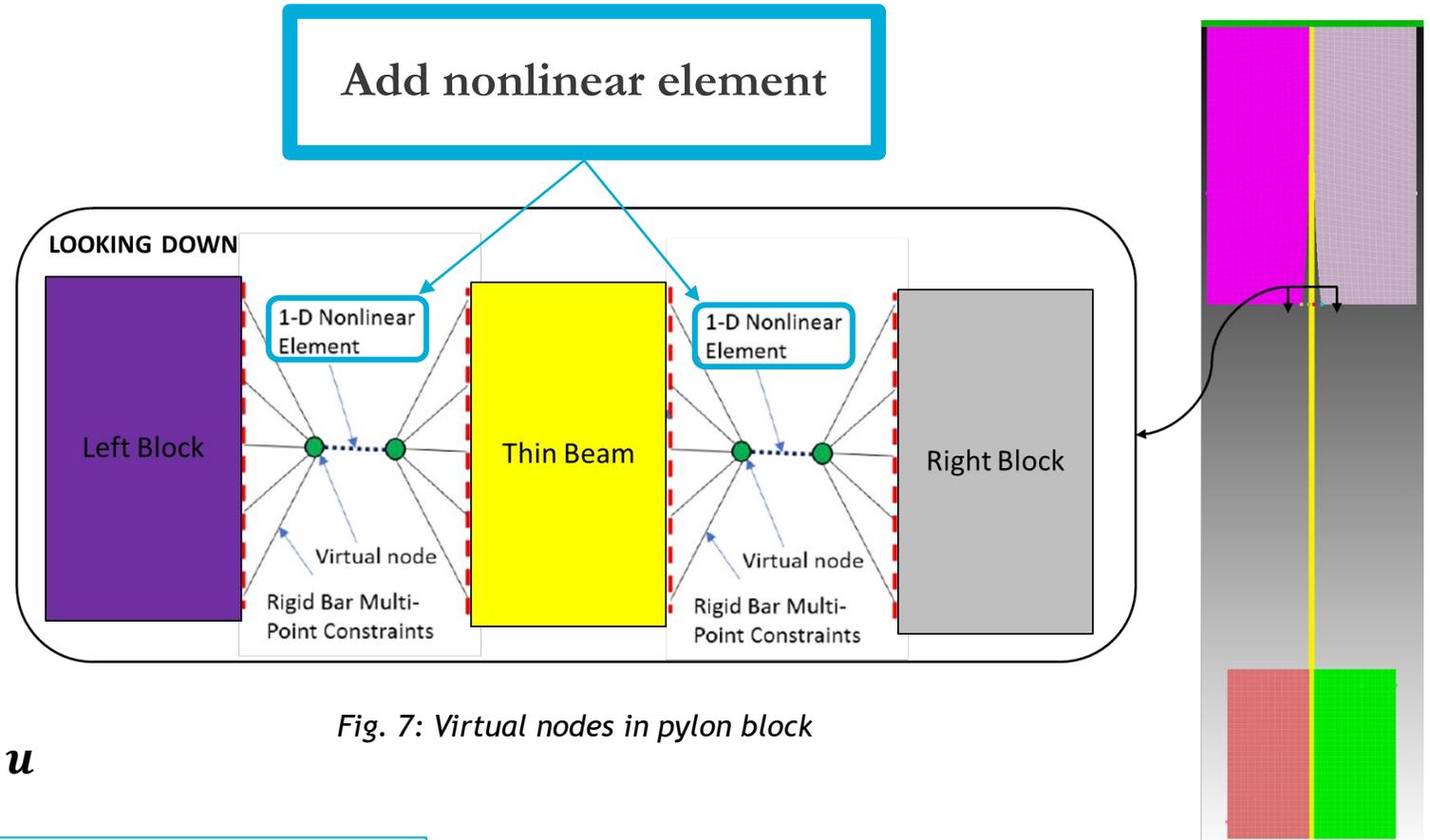


Fig. 7: Virtual nodes in pylon block

Nonlinear Normal Mode (NNM) Theory



- For an unforced, undamped system, an NNM is defined as a **response that is periodic but not necessarily synchronous** [5-6]
- A multi-degree of freedom system will have multiple NNMs
- NNMs are often illustrated in a frequency - energy plot (FEP) (Fig. 8), which shows how a system's natural frequency changes with energy input into the system
- Each point along the NNM in the FEP corresponds to a different time-history response
- Multi-harmonic balance (MHB) is one of several numerical methods used to compute NNMs

NNMs are computed using MHB and illustrated in frequency - energy plots

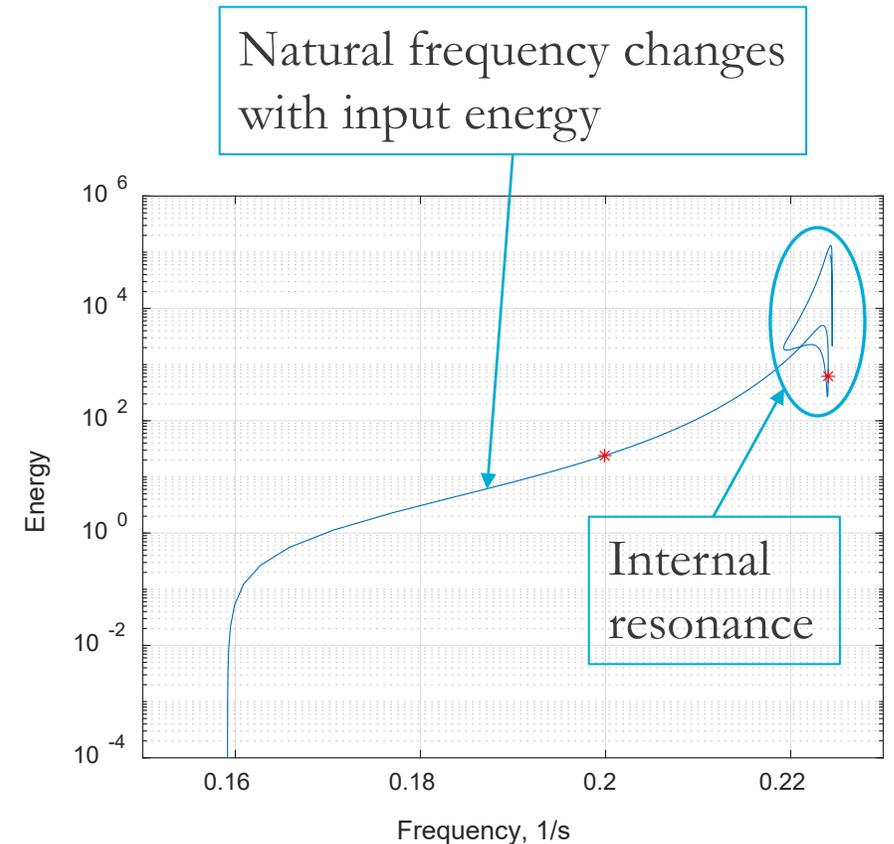


Fig. 8: Frequency - energy curve for 1st NNM of sample system

Calibrating ROM Nonlinearity

Two options were considered for nonlinear elements:

- Cubic spring element (Fig. 9)

- $f_{nl}(\Delta x) = k_{NL}(\Delta x)^3$
- Parameters:
 - k_{NL} - nonlinear spring constant

- Gap-spring element (Fig. 10)

- $f_{nl}(\Delta x) = \begin{cases} 0 & \text{for } \Delta x \leq x_{gap} \\ k_{pen}(\Delta x - x_{gap}) & \text{for } \Delta x > x_{gap} \end{cases}$
- Parameters:
 - k_{pen} - linear penalty spring constant
 - x_{gap} - gap width

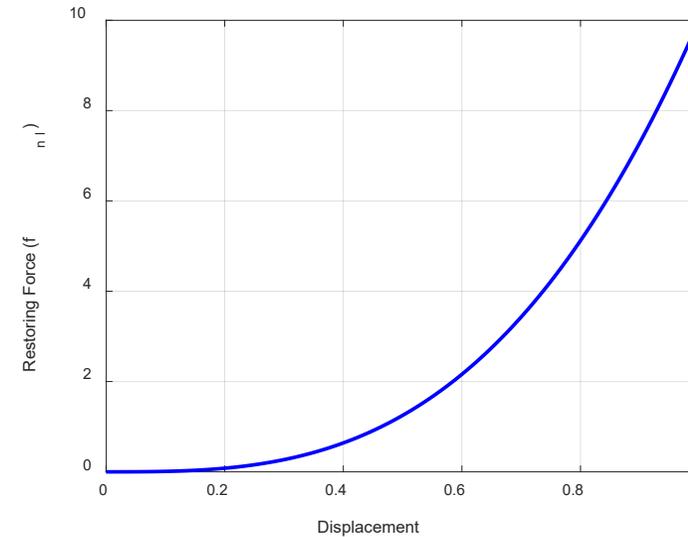


Fig. 9: f_{nl} for cubic spring element

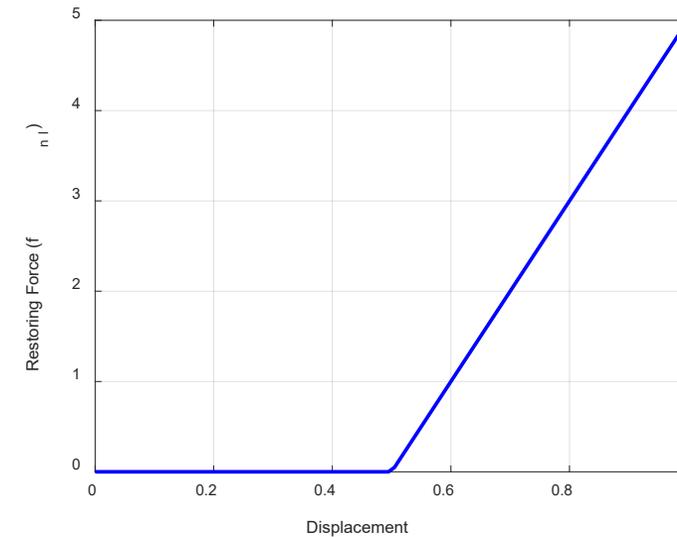


Fig. 10: f_{nl} for gap-spring element

Calibrating ROM Nonlinearity (cont.)



With cubic spring (Fig. 11) and gap-spring (Fig. 12) elements, NNM backbone curves were determined and compared to experimental data

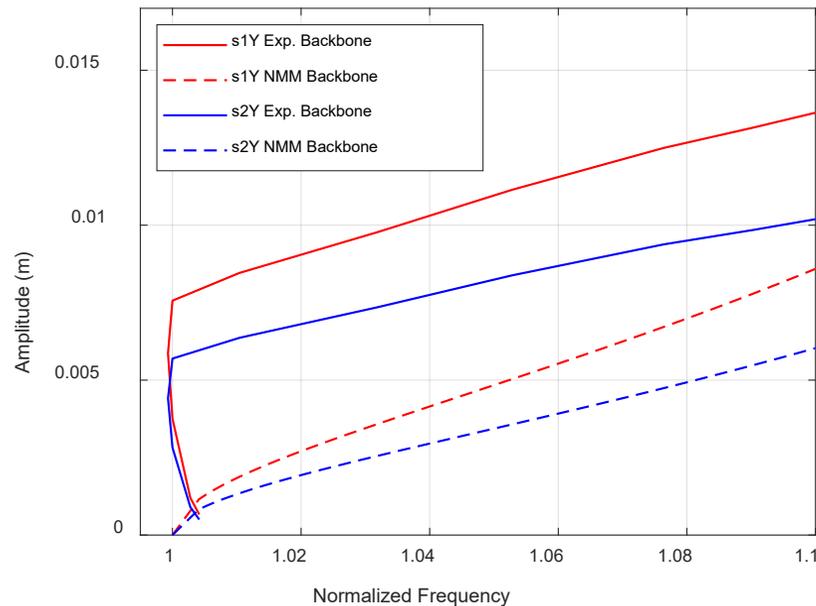


Fig. 11: Cubic spring element backbone comparison

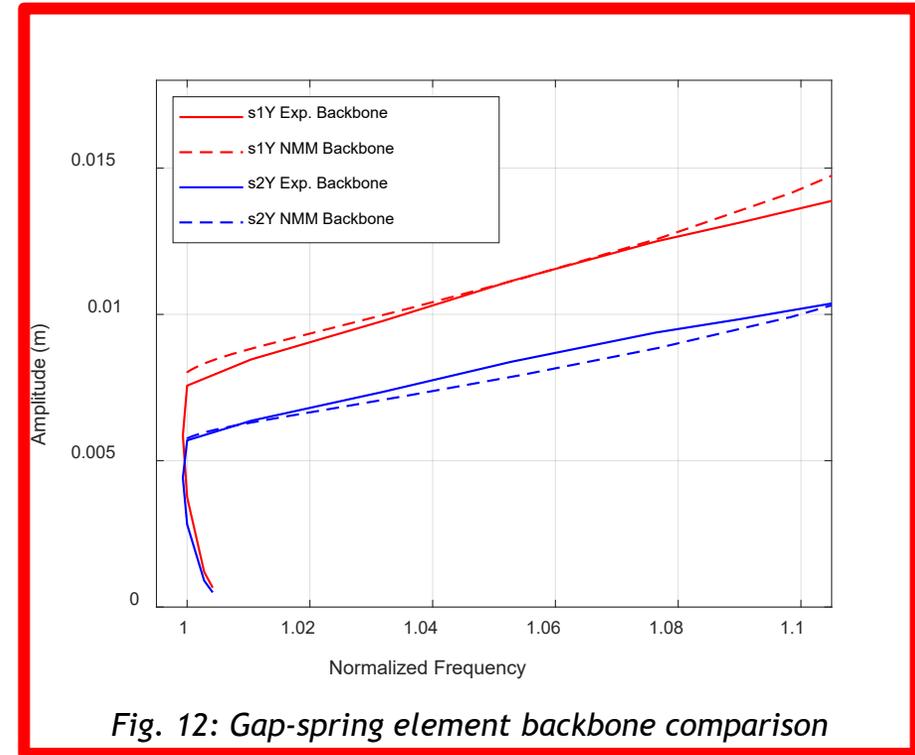
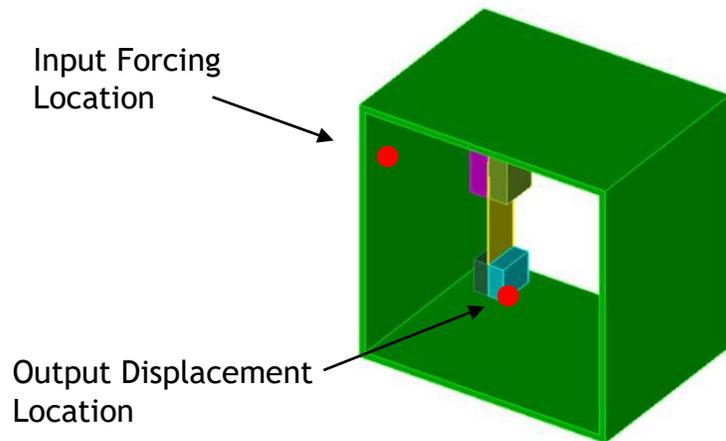


Fig. 12: Gap-spring element backbone comparison

Selected: $k_{pen} = 7 * 10^4 \text{ N/m}$
Gap-spring element $x_{gap} = 0.68 \text{ mm}$

A stepped sine test simulation was performed to verify that the gap-spring nonlinearity accurately captures the nonlinear dynamics in the pylon-fixture ROM in comparison to the NOMAD 2019 experimental results



A stepped sine test simulation will verify if the calibrated ROM is in agreement with the experimental data

Fig. 13: Fixture-pylon system with marked input and output nodes

Stepped Sine Validation (cont.)



- Despite some variation in stiffness effects, the simulation results compared relatively well with the experimental results
- Nearly all linear-peak regions occurred at a slightly higher frequency and most nonlinear-peaks were slightly smaller in magnitude, compared to the experimental results

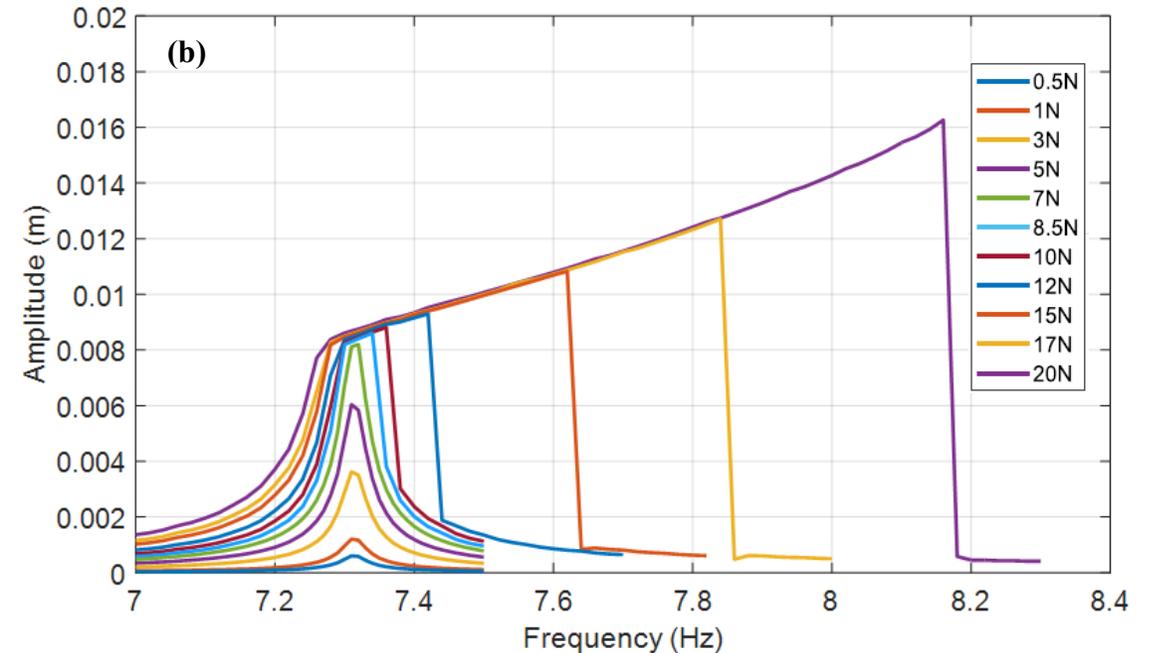
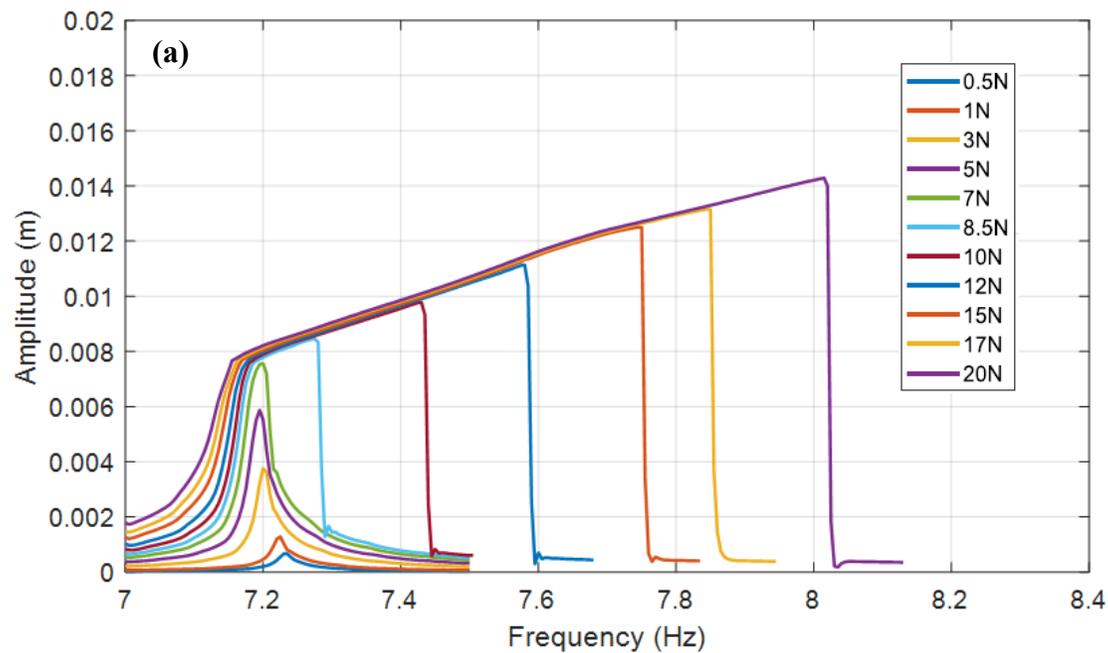


Fig. 14: Comparison of results from NOMAD 2019 experiment (a) and stepped sine simulation (b)

Stepped Sine Validation (cont.)



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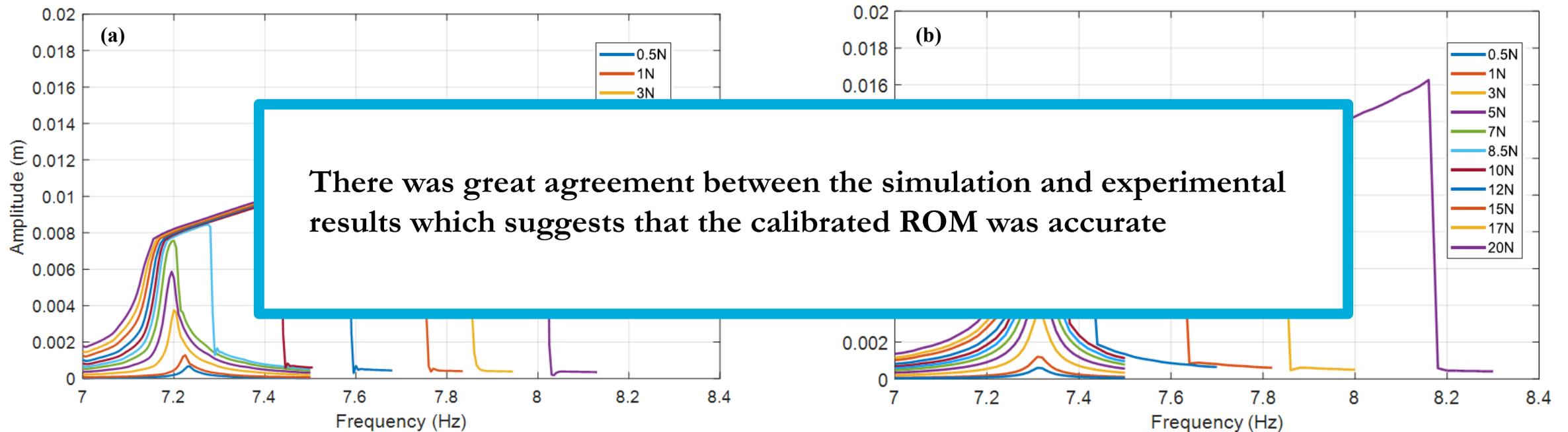


Fig. 14: Comparison of results from NOMAD 2019 experiment (a) and stepped sine simulation (b)

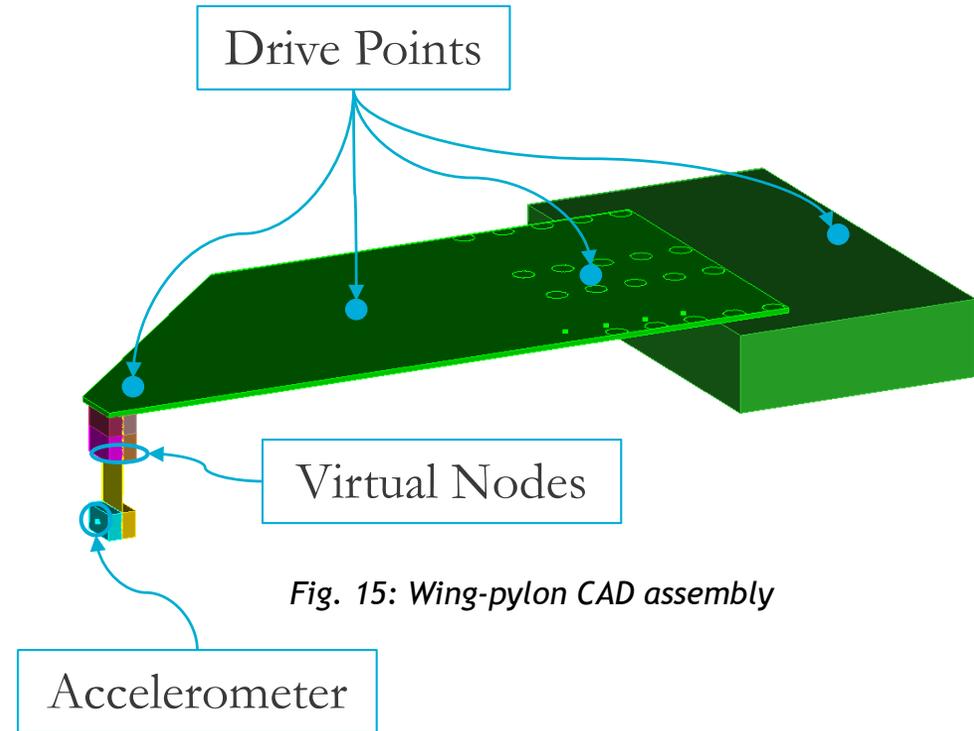


III. Full Assembly



Wing-Pylon ROM

- Next step: Attach the calibrated pylon to the wing
- Following similar methods as the fixture-pylon model, a linear finite element model of the next-level wing-pylon assembly was created
- Craig-Bampton reduction was applied using Sierra SD to obtain the linear ROM
 - DOFs for the accelerometers, virtual nodes, and drive points were retained
- The calibrated gap-spring element in the pylon block was added to the linear ROM to describe the nonlinear EOMs



Linear wing-pylon ROM from Sierra	+	Calibrated gap- spring element in pylon	=	Nonlinear EOMs
$M\ddot{x}(t) + C\dot{x}(t) + Kx(t)$		$f_{nl}\{x(t)\}$		$M\ddot{x}(t) + C\dot{x}(t) + Kx(t) + f_{nl}\{x(t)\} = u$

Mode shapes for linear wing-pylon model:

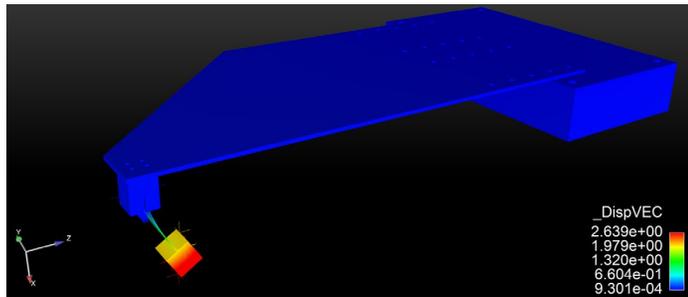


Fig. 16: Mode 1 (7.30 Hz)

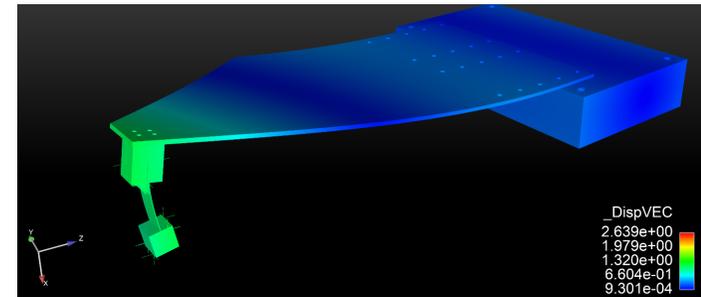


Fig. 17: Mode 2 (22.20 Hz)

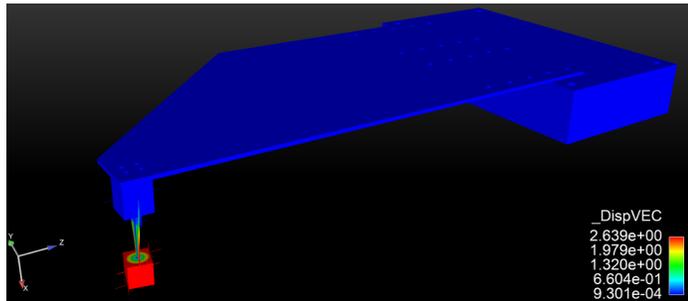


Fig. 18: Mode 3 (47.28 Hz)

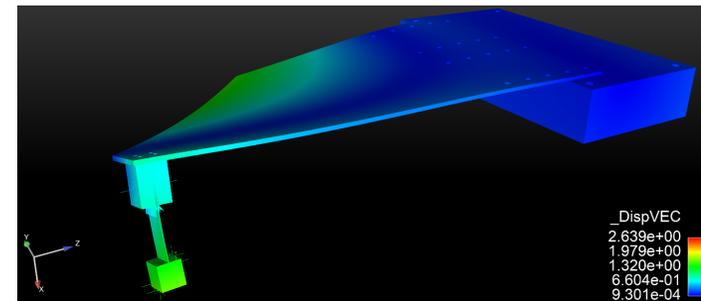


Fig. 19: Mode 4 (49.22 Hz)

Note: mode numbers refer to elastic modes

- The MHB method was utilized to identify NNMs and any possible internal resonances for the calibrated wing-pylon ROM
- Mode 2 was of interest because the bending of the wing resulted in bending of the pylon beam which produced large displacements in the lower pylon block
- Large displacements in the pylon initiated the nonlinear behavior in the gap-spring element

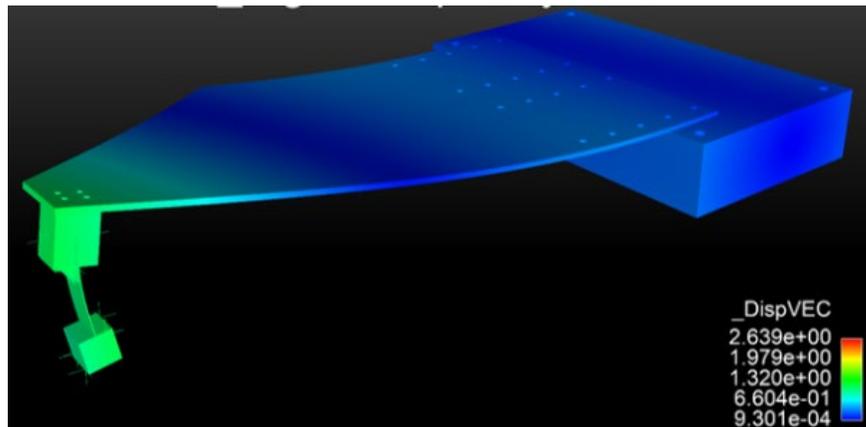


Fig. 20: Mode 2 (22.20 Hz)

Mode 2 was considered for further investigation based on the large wing and pylon bending mode shapes

Multi-Harmonic Balance Method (cont.)



- NNM 2 contained a small frequency shift which remained extremely close to linear mode 2 resonant frequency
- This can easily be overlooked if only a linear analysis is considered thus reinforcing the significance of nonlinear analyses
- An internal resonance was identified on a tongue of NNM 2

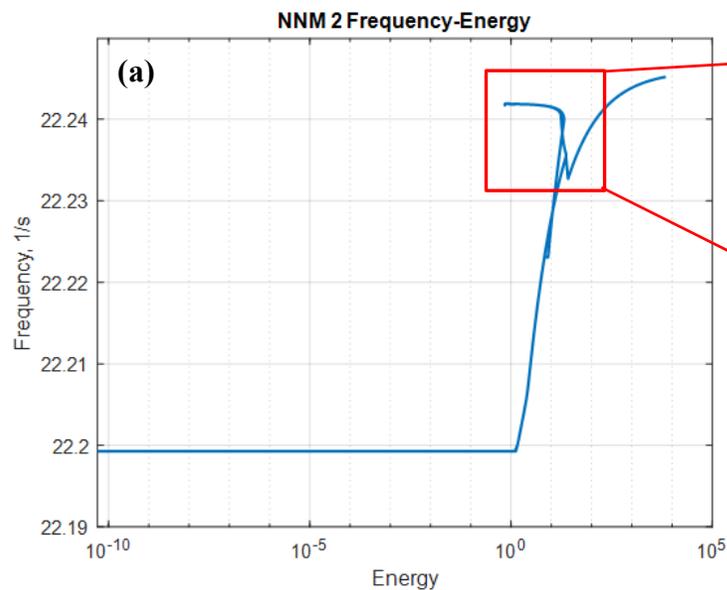


Fig. 21: NNM 2 of the Wing-Pylon Assembly

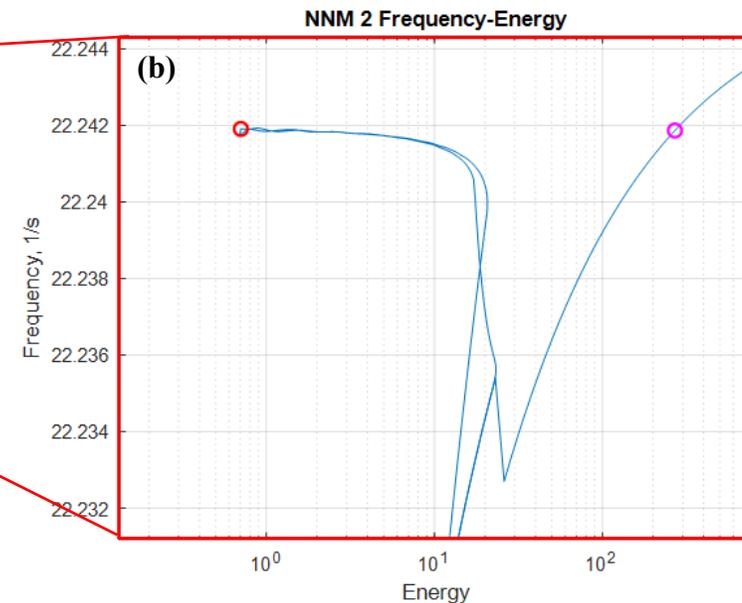


Fig. 22: NNM 2 with Identified Internal Resonance and Single Harmonic Points

Multi-Harmonic Balance Method (cont.)



- A 1:5 internal resonance was identified between NNM 2 and 7 on the wing-pylon ROM; the red point in (a) is the tongue of the internal resonance between the two NNM's
- The internal resonance can easily be seen in the displacement time-history (b) where multiple ratios of 1:5 harmonics exist
- Single harmonic motion exists (c) in NNM 2 as well which is described by the magenta point in (a)

NNM 2 remained very close to its linear mode and additionally contained a 1:5 internal resonance with NNM 7

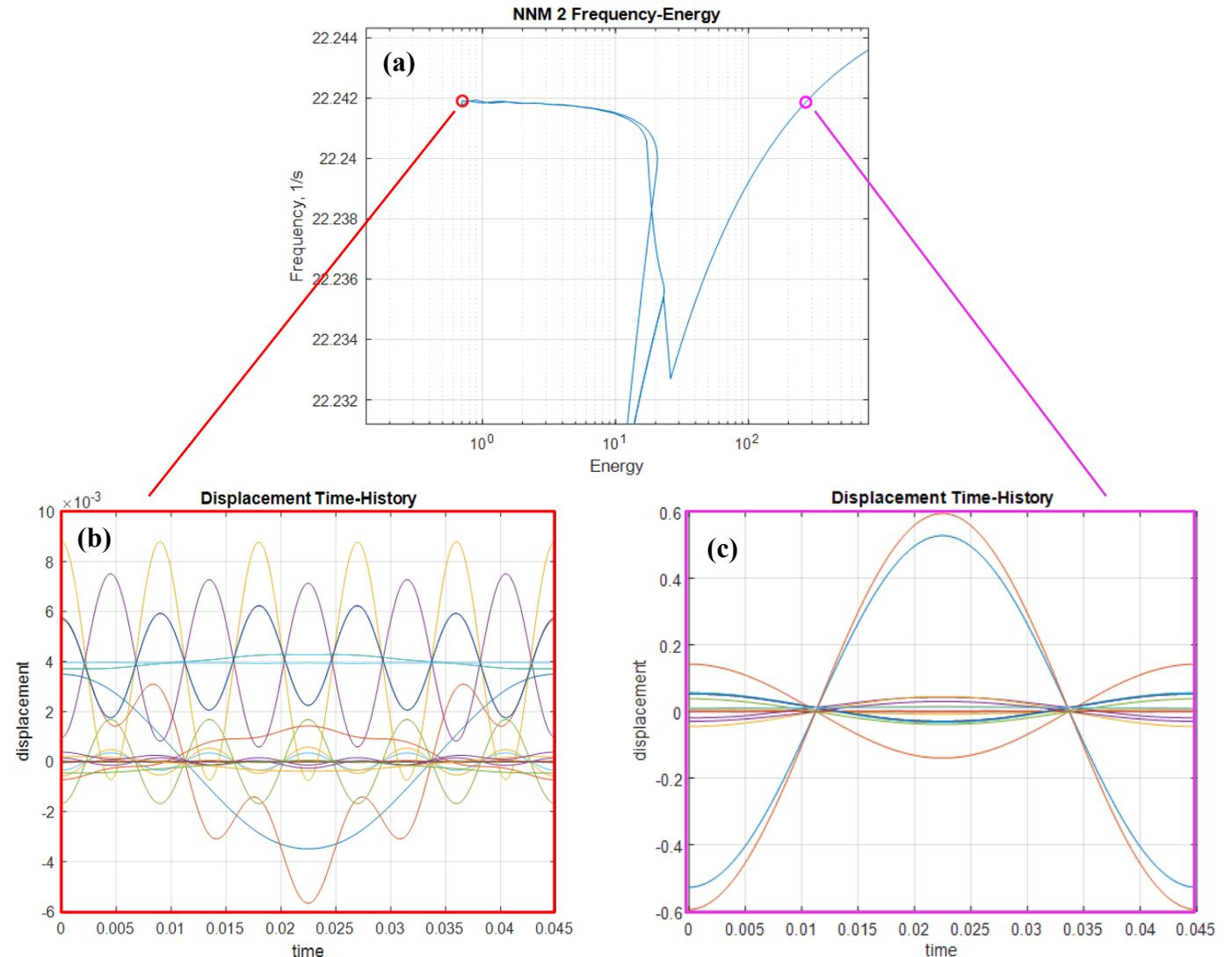


Fig. 23: Displacement Time-Histories of Identified Internal Resonance and Single Harmonic Motion

- The modal interaction between the NNM's 2 and 7 are depicted in plot (b) where NNM 7 was scaled down by an integer of 5 and only computed to the 5th harmonic (there are more harmonics and internal resonances on NNM 7)
- This essentially means when mode 2 is excited mode 7 can experience large displacement amplitude responses

(a)

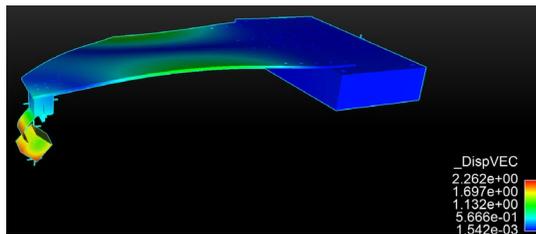
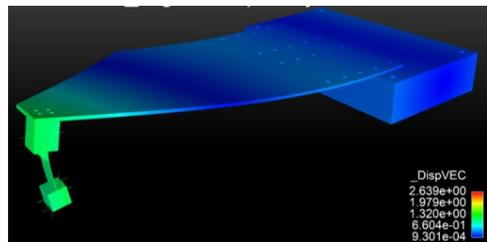


Fig. 24: Linear Modes 2 and 7 Mode Shapes

(b)

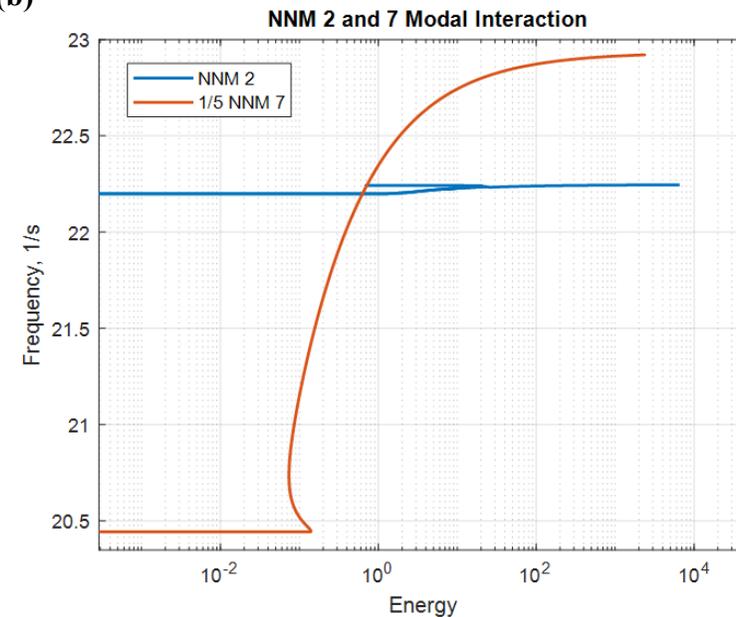


Fig. 25: NNM 2 and 7 Modal Interaction

(c)

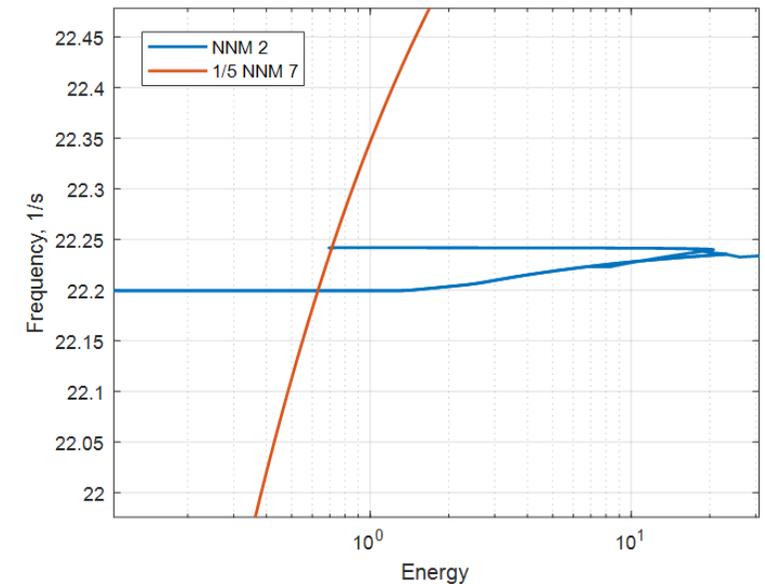


Fig. 26 NNM 2 and 7 Internal Resonance Crossing

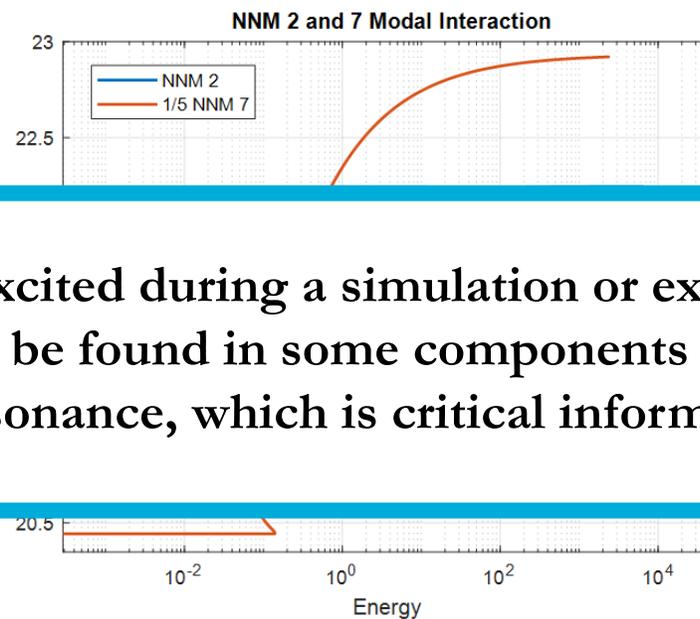


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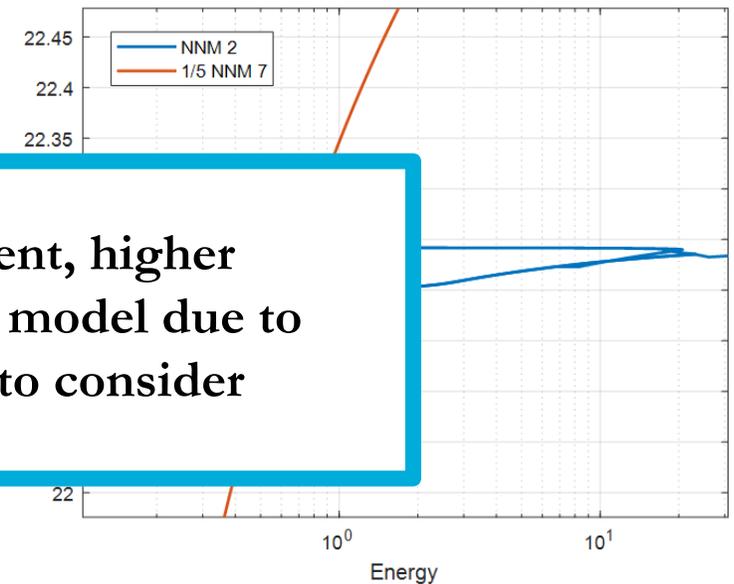
(a)



(b)



(c)



If NNM 2 is excited during a simulation or experiment, higher harmonics can be found in some components of the model due to the internal resonance, which is critical information to consider

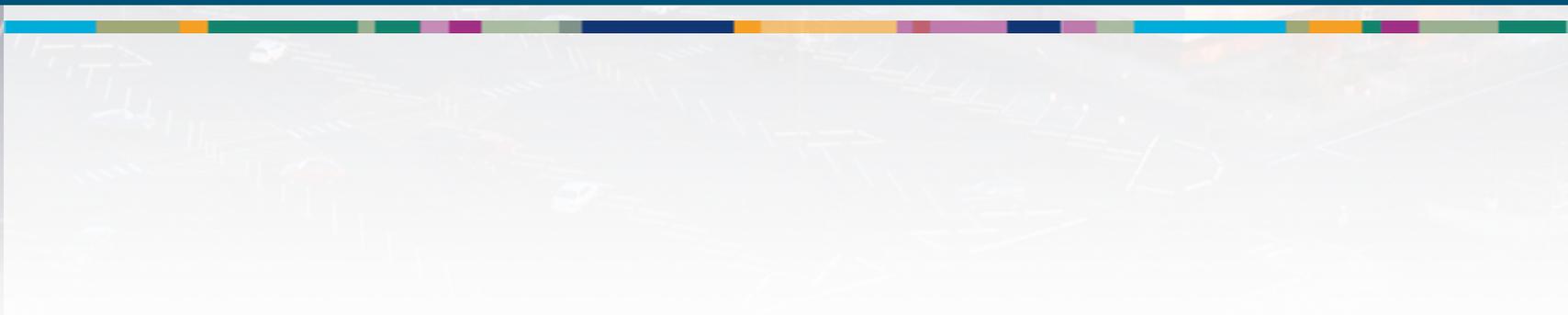
Fig. 24: Linear Modes 2 and 7 Mode Shapes

Fig. 25: NNM 2 and 7 Modal Interaction

Fig. 26 NNM 2 and 7 Internal Resonance Crossing



IV. Virtual Experiments



To account for physical limitations of the shaker, a previously calibrated electro-mechanical shaker model was substructured to the wing-pylon ROM for simulated experiments using the force appropriation method

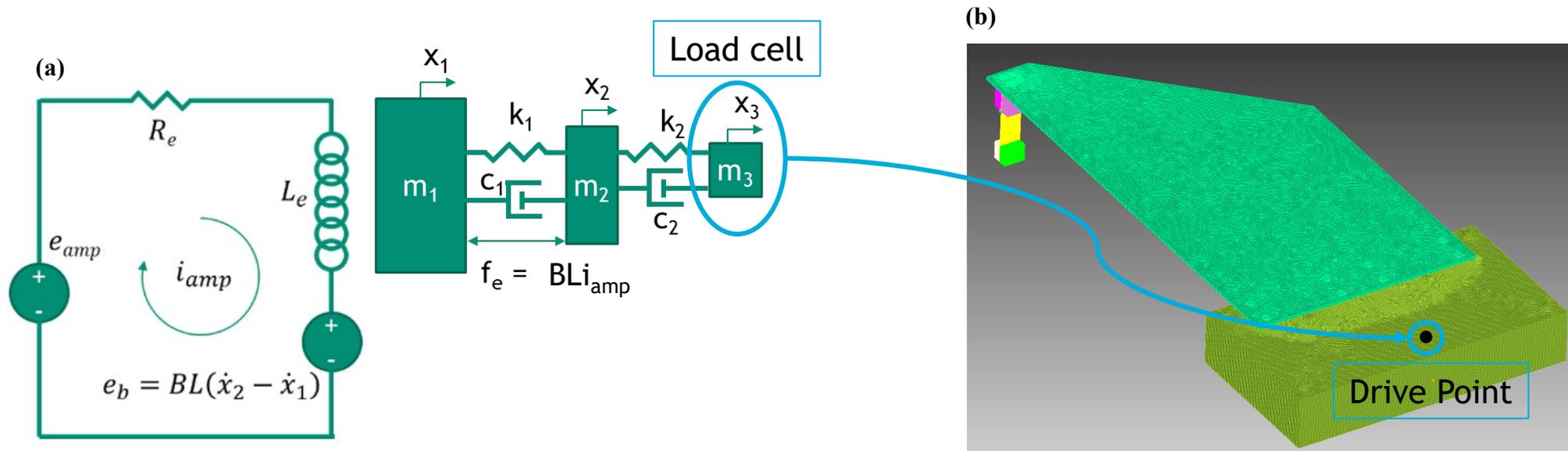


Fig. 27: Virtual shaker model (a) and wing-pylon finite element model (b)

Note: Shaker input voltage is the only input to the substructured shaker, wing, pylon system

Force Appropriation Method



- Phase lag quadrature criterion: A single NNM is isolated if the structure vibrates with a phase lag of 90° with respect to the input signal
- Force appropriation testing relies on the phase lag quadrature criterion
 - The structure is excited at different forcing frequencies until a 90° phase difference is achieved
 - NNMs can be identified one at a time using this method
- Simulated force appropriation experiments were performed for the wing-pylon assembly
 - A controller varied the frequency of the shaker input voltage until quadrature was achieved
 - The amplitude of the input voltage was then increased and the process repeated; thus constructing the frequency-energy plot (FEP) for NNMs of interest

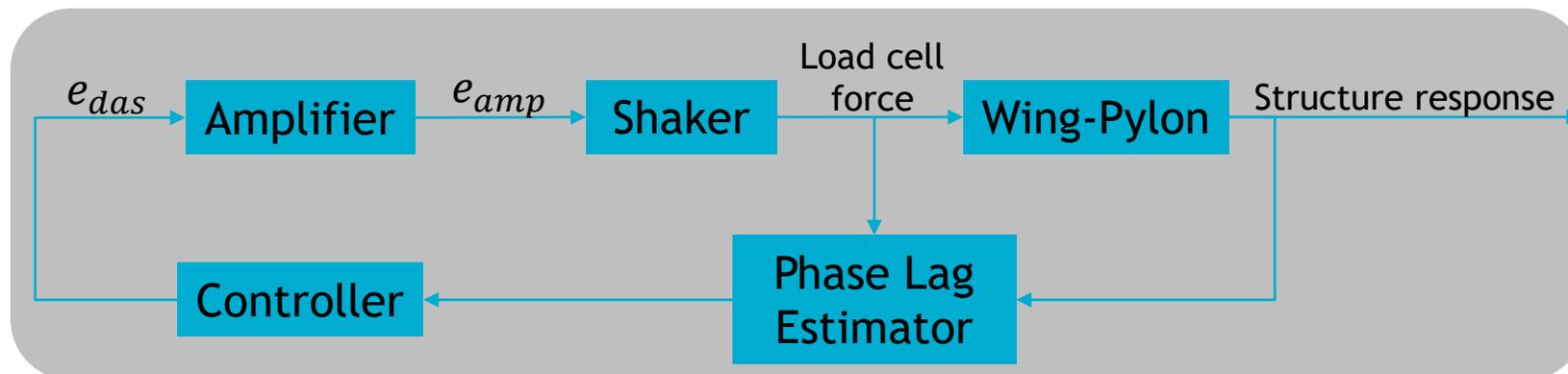


Fig. 28: Block diagram of force appropriation testing

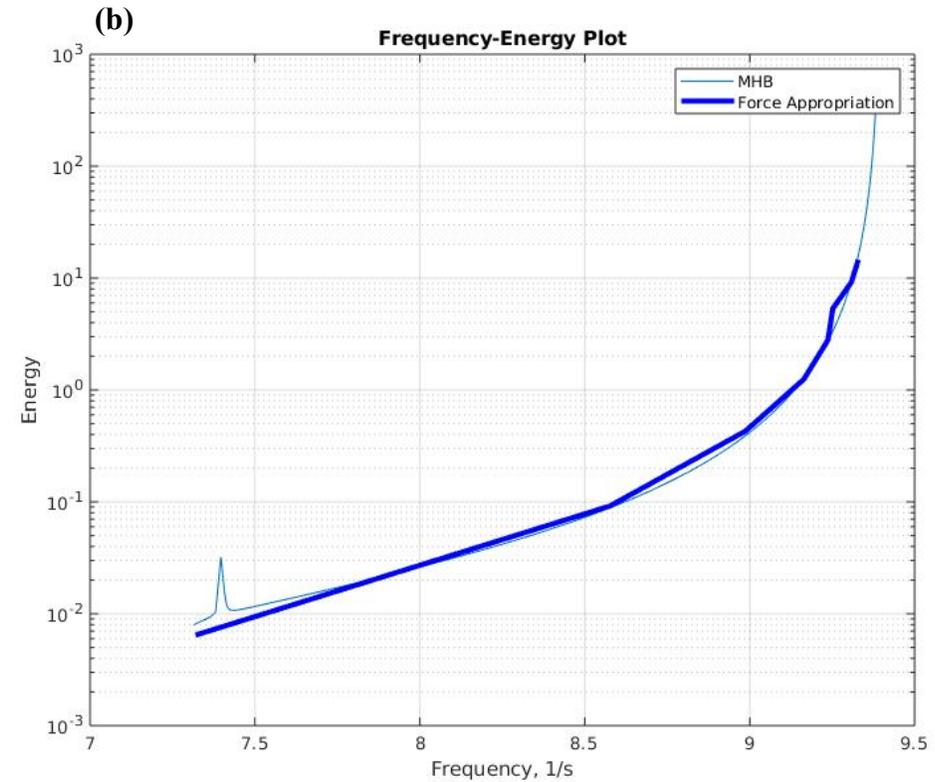
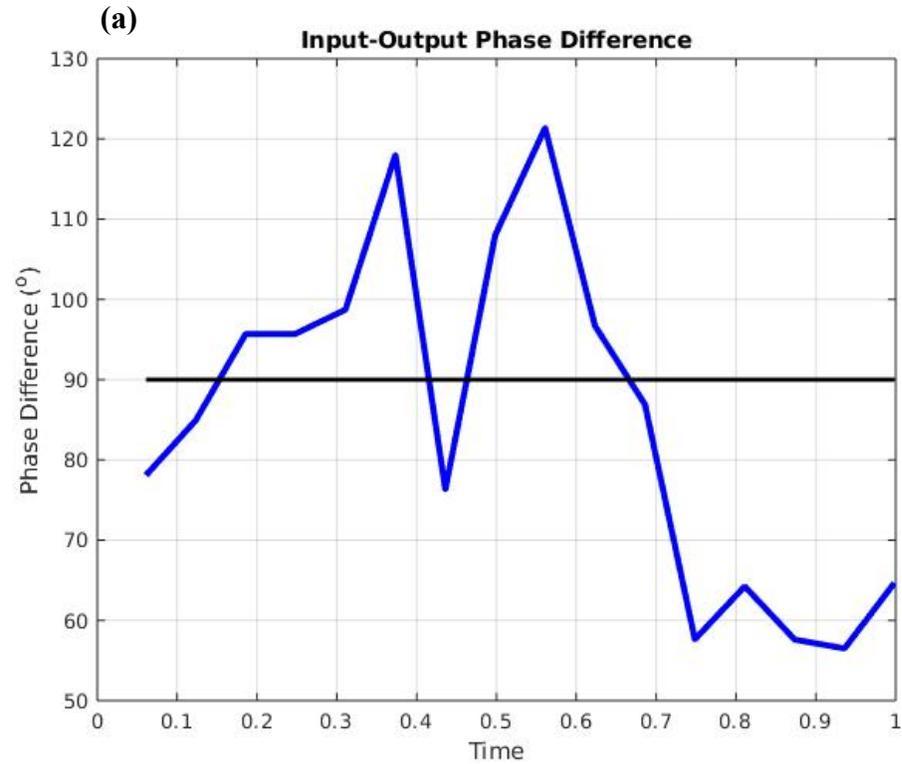
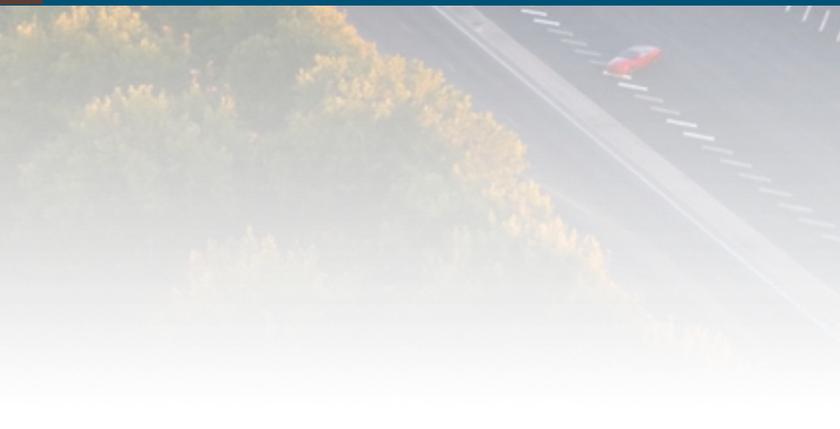


Fig. 29: NNM 1 phase lag quadrature quality (a) and FEP (b)

Further work needs to be conducted to achieve better quadrature



V. Conclusions





Results

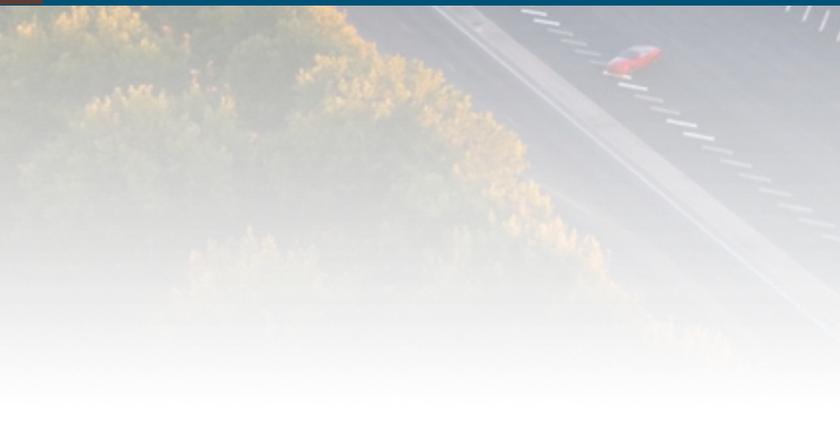
- NNMs were successfully characterized using computational methods such as force appropriation and multi-harmonic balance
- Models were accurately validated against experimental data and finite element software
- It was shown that the study of NNMs can yield insights into nonlinear systems, such as the presence and behavior of internal resonances as well as the frequency-energy dependence of nonlinear modes
- To simulate a physical experiment, a calibrated shaker model was substructured to the wing-pylon model

Future Work:

- Fine-tune simulation model to accurately simulate second and higher modes
- Experimental testing of the physical wing-pylon assembly to validate NNMs and internal resonances between different combinations of modes
- Further investigations can be conducted on the effect of other system parameters such as wing length



THANK YOU





- [1] Cooper, S.B., et al. *Investigating Nonlinearities in a Demo Aircraft Structure Under Sine Excitation*. 2020. Cham: Springer International Publishing.
- [2] Ligeikis, C., et al., Modeling and Experimental Validation of a Pylon Subassembly Mockup with Multiple Nonlinearities, in 38th International Modal Analysis Conference (IMAC XXXVIII), 2020, Houston, TX.
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- [6] Haller, G., Ponsioen, S., Nonlinear normal modes and spectral submanifolds: Existence, uniqueness, and use in model reduction. *Nonlinear Dynamics*, 2016.
- [7] T. Detroux, L. Renson, L. Masset, and G. Kerschen, "The harmonic balance method for bifurcation analysis of large-scale nonlinear mechanical systems," *Computer Methods in Applied Mechanics and Engineering*, vol. 296, pp. 18-38, 2015/11/01/ 2015, doi: <https://doi.org/10.1016/j.cma.2015.07.017>

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